# Analysis, Comparison, and Experimental Validation of a Class AB Voltage Follower With Enhanced Bandwidth and Slew Rate 

Anindita Paul ${ }^{\bullet}$, Member, IEEE, Jaime Ramírez-Angulo ${ }^{( }$, Fellow, IEEE, and Antonio Torralba ${ }^{\circledR}$, Senior Member, IEEE


#### Abstract

This paper describes a bandwidth (BW)- and slew rate (SR)-enhanced class AB voltage follower (VF). A thorough small signal analysis of the proposed and a state-of-the-art AB -enhanced VF is presented to compare their performance. The proposed circuit has $50-\mathrm{MHz} \mathrm{BW}, 19.5-\mathrm{V} / \mu \mathrm{s} \mathrm{SR}$, and a BW figure of merit of $41.6(\mathrm{MHz} \times \mathrm{pF} / \mu \mathrm{W})$ for $C_{L}=50 \mathrm{pF}$. It provides 13 times higher current efficiency and 15 times higher BW than the conventional VF with equal $60-\mu \mathrm{W}$ static power dissipation. The experimental and simulation results of a fabricated test chip in the $130-\mathrm{nm}$ CMOS technology validate the proposed circuit.


Index Terms-Analog integrated circuits, CMOS technology, MOSFET circuits, negative feedback, voltage follower (VF), wide bandwidth (BW).

## I. Introduction

THE bandwidth (BW) of the CMOS conventional voltage follower (CNV-VF), shown in Fig. 1, is given approximately by $\mathrm{BW}_{\mathrm{CNV}}=g_{m 1} / 2 \pi C_{L}$, where $g_{m 1}$ is the transconductance of $M_{1}$ and $C_{L}$ is the load capacitance. The negative slew rate $\left(\mathrm{SR}^{-}\right)$of the circuit is limited by the bias current $I_{B}$ to a value $\mathrm{SR}^{-}=I_{B} / C_{L}$, while the positive slew rate $\left(\mathrm{SR}^{+}\right)$can have a relatively large value, since the maximum positive output current is not limited by $I_{B}$. In practice, a symmetrical slew rate ( SR ) is desirable, since the lowest of the positive and negative SRs limits the large signal speed. This means that in practice, the SR corresponds to min $\left\{\mathrm{SR}^{+}\right.$, $\mathrm{SR}^{-}$\}. Both the SR and the BW can be increased at the expense of increasing $I_{B}$ and consequently the static power dissipation. In the modern submicrometer CMOS technology, low power consumption is a key requirement for increasing the

[^0]

Fig. 1. CNV-VF.
battery life of portable systems [1]-[3]. Class AB VFs (CNV-$\mathrm{AB}-\mathrm{VFs}$ ) can boost the maximum negative output current (and consequently $\mathrm{SR}^{-}$) without increasing the static power dissipation essentially. Till date, many different CNV-ABVFs have been reported that have improved the SR without improving the BW. Often, the desired class AB operation is achieved at the expense of increasing the supply voltage, the power dissipation, circuit complexity, and the silicon area. A comprehensive survey of buffers/VFs can be found in [4]. For high-speed applications, both the SR and the BW are equally important (see discussion in Section V). In this paper, we propose a simple and power efficient CNV-ABVF. The proposed CNV-AB-VF dissipates the same quiescent power as a CNV-VF but has much higher SR and BW. Three figures of merits can be used to characterize and compare the performance of VFs. First, the current enhancement figure of merit, $\mathrm{FOM}_{\mathrm{CE}}=I_{\mathrm{outMAX}} / I_{Q \text { total }}$ [5]-[7], where $I_{\text {outMAX }}$ is the maximum output current and $I_{Q \text { total }}$ is the total quiescent current. This is related to the SR improvement and the large signal performance of the circuit. Second, the BW figure of merit [6]-[8], $\mathrm{FOM}_{\mathrm{BW}}=\mathrm{BW}(\mathrm{MHz}) C_{L}(\mathrm{pF}) / P^{Q}(\mu \mathrm{~W})$, where $P^{Q}$ is the total quiescent power dissipation of the circuit. Since $\mathrm{FOM}_{\mathrm{CE}}$ determines the speed limitation for large signals and $\mathrm{FOM}_{\mathrm{BW}}$ limits the speed of small signals, a third global speed figure of merit [6], [7] can also be defined that corresponds to the geometric mean of the previous two figures of merit $\mathrm{FOM}_{\mathrm{GLB}}=\left(\mathrm{FOM}_{\mathrm{CE}} \mathrm{FOM}_{\mathrm{BW}}\right)^{1 / 2}$.


Fig. 2. CMOS CNV-AB-VFs. (a) CMOS FVF reported in [9]. (b) CMOS CNV-AB-VF reported in [10]. (c) Proposed CMOS CNV-AB-VF.

## II. Proposed Voltage Follower

Fig. 2(a) shows a class AB flipped VF (FVF) reported in [9] with an additional transistor $M_{1 \mathrm{AB}}$, which operates as a CNV-VF and can improve $\mathrm{SR}^{+}$. However, its output swing is limited by the gate-source voltage of $M_{2}$. The input/output peak-to-peak swing is given by $V_{\text {inpp }}=V_{T}-V_{\mathrm{DS} s \mathrm{at}}$, where $V_{T}$ is the threshold voltage of the transistor. This swing is very small and independent of the supply voltage. This is a very serious limitation, since in the modern technology, lower values of threshold voltage ( $V_{T} \sim 0.4 \mathrm{~V}$ ) are used. Maximum peak output signals of the circuit in [9] with a low distortion are on the order of only 0.15 V . Fig. 2(b) shows a CNV-$\mathrm{AB}-\mathrm{VF}(\mathrm{CNV}-\mathrm{AB}-\mathrm{VF})$ reported in [10] that has a resistor $R_{L}$ inserted between the drain of $M_{1}$ and $V_{\mathrm{DD}} . M_{1}$ and $M_{2}$ have equal quiescent currents $I_{B}$. It can be considered as a dynamic FVF without the swing limitations of the circuit in Fig. 2(a), since the dc operating points at node $V_{x}$ is independent of
the dc operating point at node $V_{Y}$ and they are connected in the presence of ac signals. The circuit in Fig. 2(b) operates as follows: transient variations in $V_{\text {in }}$ generate variations in $V_{x}$ which are $180^{\circ}$ out of phase with $V_{\mathrm{in}}$. These variations are transferred from node $V_{X}$ to node $V_{Y}$ using a capacitor $C_{\text {BAT }}$ that acts as a floating battery for fast changes in $V_{X}$. Furthermore, $R_{\text {large }}$ and $C_{\text {BAT }}$ form a high-pass circuit for signals passing from $V_{X}$ to $V_{Y}$. This changes the current of $M_{2}$ as a function of the variations in $V_{\mathrm{in}}$. Negative (positive) values of $V_{\text {in }}$ leads to positive (negative) values in $V_{X}$ and $V_{Y}$, which increase (decrease) the dynamic drain current of $M_{2}$. This leads to maximum negative output currents that can be essentially larger than $I_{B}$ and therefore much higher negative SR than the CNV-VF. An additional advantage of the SR enhancement circuit ( $R_{L}, R_{\text {large }}$, and $C_{\mathrm{BAT}}$ ) is that the local negative feedback through $C_{\text {BAT }}$ in the presence of ac signal decreases the output impedance of the follower by the gain $1+g_{m 2} R_{\mathrm{L}}$ of the negative feedback loop. This also


Fig. 3. Small signal analysis of CNV-AB-VF [10].
helps to enhance the BW of the follower, as explained in Section III. In the circuit shown in Fig. 2(b), both the BW and the maximum negative output current (and $\mathrm{SR}^{-}$) increase with $R_{L}$. However, the increase of $R_{L}$ leads to a decrease in the maximum positive output current (and in the $\mathrm{SR}^{+}$), since it is in series with the drain of $M_{1}$. This does not allow optimizing $\mathrm{SR}^{+}, \mathrm{SR}^{-}$, and BW simultaneously. The proposed VF is shown in Fig. 2(c). It overcomes the limitations of the FVF shown in Fig. 2(a) and of the CNV-AB-VF shown in Fig. 2(b). It is derived by merging the conventional follower in Fig. 1 with the circuit in Fig. 2(b). This is done by adding a transistor $M_{1 \mathrm{AB}}$ connected as a CNV-VF. $M_{1 \mathrm{AB}}$ can provide a large positive output current which is independent of the value of $R_{L}$. To maintain equal quiescent power dissipation as the CNV-AB-VF and the CNV-VF, the current mirror ratio $W_{2 P} / W_{B}$ of the proposed VF is 1:1 where $W_{2 P}$ and $W_{B}$ are the widths of $M_{2 P}$ and $M_{B}$. From this point, the proposed circuit in Fig. 2(c) will be denoted as "PRP-AB-VF." As it is shown in Section III, the PRP-AB-VF can deliver simultaneously nearly symmetric and large maximum positive and negative output currents and exhibits moderate-to-high BW enhancement with little area overhead and with the same static power dissipation, as the CNV-VF in Fig. 1. In this paper, the PRP-AB-VF is intended to be used as a buffer for amplifiers. In order to perform a comparison, the small signal analysis of the circuit in [10, Fig. 2(b)] is also included here, since [10] does not include the analysis of the circuit's BW. The focus of this paper is to demonstrate that the proposed circuit has significantly enhanced BW with respect to the circuit shown in Fig. 2(b) and simultaneously high symmetrical SR. The circuit in Fig. 2(a) is not included in the comparison due to the swing limitations.

## III. Small Signal Analysis of CNV-AB-VF Circuit Reported in [10]

In this section, a small signal analysis of the CNV-AB-VF circuit in Fig. 2(b) is presented. Transistors $M_{1}$ and $M_{2}$ have equal dimensions ( $W / L$ ), the same quiescent current $I_{B}$, and the same transconductance gains $g_{m 1}=g_{m 2}=g_{m}$. At frequencies higher than $f_{0}=1 /\left(2 \pi R_{\text {large }} C_{\mathrm{BAT}}\right)$, the capacitor $C_{\text {BAT }}$ acts as a short circuit that connects nodes $V_{X}$ and $V_{Y}$ and provides dynamic negative feedback. This negative feedback helps to enhance the BW of the CNV-AB-VF follower, according to the analysis shown in the following.
Fig. 3 shows the ac equivalent circuit of Fig. 2(b) for $f \geq$ $f_{0}=1 /\left(2 \pi R_{\text {large }} C_{\mathrm{BAT}}\right)$. The closed-loop transfer function


Fig. 4. Root locus of poles of CNV-AB-VF [10] for varying open-loop gain $A_{\mathrm{OL}}=g_{m} R_{L}$.
$G_{\mathrm{CL}}(s)=\left(V_{\text {Out }} / V_{\text {in }}\right)(s)$ of the CNV-AB-VF is given by

$$
\begin{equation*}
G_{\mathrm{CL}}(s)=\frac{\left(a / C_{X} C_{L}\right)\left(1+s C_{X} g_{m 1} / a\right)}{s^{2}+2 \xi_{\mathrm{CNV}}-\mathrm{AB} \omega_{n \mathrm{CNV}-\mathrm{AB}} s+\omega_{n \mathrm{CNV}-\mathrm{AB}}^{2}} \tag{1}
\end{equation*}
$$

where

$$
\begin{aligned}
a & =\left(G_{L} g_{m 1}+g_{m 1} g_{m 2}\right) \\
g_{m 1 \mathrm{~b}} & =\left(g_{m 1}+g_{m b}\right) \\
2 \xi_{\mathrm{CNV}-\mathrm{AB}} \omega_{n \mathrm{CNV}-\mathrm{AB}} & =\left(g_{m \mathrm{lb}} / C_{L}\right)+\left(G_{L} / C_{X}\right) \\
\omega_{n \mathrm{CNV}-\mathrm{AB}}^{2} & =\left(g_{m 1 \mathrm{~b}} G_{L} / C_{X} C_{L}\right)+\left(g_{m 1 \mathrm{~b}} g_{m 2} / C_{X} C_{L}\right) \\
& =\left(g_{m 1 \mathrm{~b}} / C_{X} C_{L}\right)\left(G_{L}+g_{m 2}\right) .
\end{aligned}
$$

In this analysis, the zero created by $C_{\mathrm{gs}}$ of $M_{1}$ is ignored. The zero has a frequency $f_{\text {Zcgs } 1}=(1 / 2 \pi)\left(g_{m 1} / C_{g s 1}\right)$ that has a very high value $(\sim \mathrm{GHz})$ and thus does not affect the response in the range of operation of the follower. Substituting $g_{m 2}=g_{m 1}=g_{m}$ in (1), it can be observed that the closedloop gain $G_{\mathrm{CL}}$ has a zero at $\omega_{Z}=\left(G_{L}+g_{m}\right) / C_{X}$ and two poles. As the capacitance at node $V_{X}$, given by $C_{X}$, is very small, this zero is also at very high frequency. Hence, the effect of this zero is assumed to be negligible. The poles can be either real or complex conjugate, depending on the value of the dc open-loop gain $A_{\mathrm{OL}}=g_{m} R_{L}$ of the negative feedback loop. For example, a root locus plot of the poles of $G_{\mathrm{CL}}$ as a function of $g_{m} R_{L}$ is shown in Fig. 4. It is obtained for a typical design in the $130-\mathrm{nm}$ CMOS technology with $I_{B}=50 \mu \mathrm{~A}$, dual supply voltages of $\pm 0.6 \mathrm{~V}, C_{L}=20 \mathrm{pF}$, and transistor dimensions $W / L=15 / 0.15(\mu \mathrm{~m})$. The forgoing parameters result in $g_{m}=836 \mu \mathrm{~A} / \mathrm{V}, r_{o}=25 \mathrm{k} \Omega$, and $C_{x} \approx 0.1 \mathrm{pF}$. This plot reveals that for values $g_{m} R_{L}<6$, the poles are on the negative real axis. As the gain $g_{m} R_{L}$ continues to increase, the poles move toward each other and become complex conjugate (for example for the values of $g_{m} R_{L}>6$ ) and the BW can be obtained by [11]

$$
\begin{equation*}
\mathrm{BW}=\omega_{3 \mathrm{~dB}}=\omega_{n} \sqrt{\left(1-2 \zeta^{2}\right)+\sqrt{\left(4 \xi^{4}-4 \xi^{2}+2\right)}} \tag{2}
\end{equation*}
$$



Fig. 5. BW of CNV-AB-VF and CNV-VF as a function of $g_{m} R_{L}$.

For the CNV-AB-VF, $\xi$ and $\omega_{n}$ are given, respectively, by

$$
\begin{align*}
\xi_{\mathrm{CNV}-\mathrm{AB}} & =\left[\left(g_{m \mathrm{lb}} / C_{L}\right)+\left(G_{L} / C_{X}\right)\right] / 2 \omega_{n \mathrm{CNV}-\mathrm{AB}} \\
& =1 / 2 Q  \tag{3}\\
\omega_{n \mathrm{CNV}-\mathrm{AB}} & =\sqrt{\left(G_{L}+g_{m}\right)\left(g_{m \mathrm{lb}} /\left(C_{X} C_{L}\right)\right)} \tag{4}
\end{align*}
$$

As $g_{m} R_{L}$ increases, the BW (see Fig. 5) and the $Q$ factor increase (the damping ratio $\zeta$ decreases as shown in Fig. 4). To avoid peaking in the frequency response (or overshoot in the transient response), values $Q<0.707$ or $\zeta>0.707$ need to be selected. For $\zeta=0.707$, the maximum BW $=\omega_{n} / 2 \pi$ without overshoot in the transient response is achieved. In this example, from the root locus, a value $g_{m} R_{L}=8.3$ leads to $\xi_{\mathrm{CNV}-\mathrm{AB}}=0.73$ and $Q=0.68$. Thus, the corresponding BW can be obtained from (2) inserting the values of $\xi=0.73$ and $\omega_{n}$ from (4). For $g_{m}=836 \mu \mathrm{~A} / \mathrm{V}^{2}, g_{m \mathrm{lb}}=g_{m}(1+\eta)$, $\eta=0.2$ [12], $C_{X}=0.1 \mathrm{pF}, C_{L}=20 \mathrm{pF}$, and $R_{L}=10 \mathrm{k} \Omega$, the BW is $\mathrm{BW}_{\mathrm{CNV}-\mathrm{AB}-\mathrm{VF}}=105 \mathrm{MHz}$, which is 16 times higher than the BW of the CNV-VF given by $B W_{C N V-V F}=$ $g_{m} / 2 \pi C_{L}=6.6 \mathrm{MHz}$. Fig. 5 shows that the BW continues to increase until $g_{m} R_{L}=16$. However, it is not desirable to increase $g_{m} R_{L}$ for the values of $Q>0.707$ in order to avoid overshoot in the transient response and peaking in the frequency response. A drawback of the CNV-AB-VF is that when $R_{L}$ increases even for values $Q<0.707$, the voltage drop across $R_{L}$ increases and causes $V_{X}$ and $V_{\mathrm{DS}}$ of the $M_{1}$ transistor to decrease. This leads to a significant decrease in the maximum positive output current and in turn to a decrease in the positive SR of the circuit. Fig. 6 shows the maximum positive output current of the $\mathrm{CNV}-\mathrm{AB}-\mathrm{VF}$ as a function of $R_{L}$. It can be observed that the maximum output current decreases by a factor of 10 from $1100 \mu \mathrm{~A}$ for $g_{m} R_{L}=0$ to $111 \mu \mathrm{~A}$ for $g_{m} R_{L}=8.3$ and $Q=0.68$. The PRP-AB-VF overcomes this problem. The small signal analysis of the PRP-AB-VF is discussed in Section IV.

## IV. Small Signal Analysis of Proposed Class AB VF

The proposed circuit shown in Fig. 2(c) can achieve simultaneously large positive and negative SRs and essentially an improved BW. This circuit has the same quiescent power dissipation as the CNV-VF and as the CNV-AB-VF. It incorporates just one additional transistor $M_{1 \mathrm{AB}}$ that acts as a CNV-VF. This transistor can provide a large positive output current


Fig. 6. Maximum positive output current for CNV-VF and CNV-AB-VF as a function of $g_{m} R_{L}$.
independent of the value of $R_{L}$ that is used to control the enhancement of the BW and the negative SR. The small signal analysis of the proposed circuit is discussed in detail in this section. The ac equivalent circuit of the PRP-AB-VF for $f>f_{o}$ is shown in Fig. 7. The proposed VF is designed for relatively large capacitive loads $C_{L}$ that satisfy $C_{L} \gg C_{\mathrm{gs}}$. Since the PRP-AB-VF was not intended for applications in oscillators where negative input resistance of the follower is important [13], [14], the effect of $C_{\mathrm{gs}}$ is ignored in the small signal analysis. As the dimension $(W / L)$ of all the transistors in Fig. 2(c) are equal, and the total bias current of the circuit is $I_{B}$, the quiescent current of $M_{1}$ and $M_{1 \mathrm{AB}}$ is $I_{B} / 2$. In the PRP-AB-VF, the sizes of all the transistors are the same as in CNV-VF and CNV-AB-VF. This maintains equal power dissipation in the three VF circuits. Hence, if transistors operate in a strong inversion, the transconductance gains $g_{m 1 \mathrm{P}}$ and $g_{m 1 \mathrm{AB}}$ of $M_{1 \mathrm{P}}$ and $M_{1 \mathrm{AB}}$ in the proposed circuit are a factor $1 / \sqrt{ } 2$ times smaller than the transconductance gain of $M_{1}$ of the CNV-VF (see Fig. 1) and of the CNV-AB-VF [see Fig. 2(b)]. Thus, $g_{m 1 \mathrm{P}}=g_{m 1 \mathrm{AB}}=g_{m} / \sqrt{ } 2$ and $g_{m 1 \mathrm{~Pb}}=$ $g_{m 1 \mathrm{ABb}}=(1+\eta) g_{m} / \sqrt{ } 2=(1.2) g_{m} / \sqrt{ } 2$. Transistors $M_{2}$ and $M_{2 p}$ in Fig. 2(b) and (c) carry equal bias currents $\left(I_{B}\right)$ and have identical dimensions in order to keep the equal power dissipation as the CNV-VF and the CNV-AB-VF circuits. Hence, their transconductance gains are equal ( $g_{m 2}=g_{m 2 \mathrm{P}}=$ $g_{m}$ ) and both the CNV-AB-VF and the PRP-AB-VF have equal open-loop gain $A_{\mathrm{OL}}=g_{m} R_{L}$. Hence, the closed-loop transfer function ( $G_{\mathrm{CLP}}=V_{\mathrm{Out}} / V_{\mathrm{in}}$ ) of the proposed VF is given by (5). This transfer function has a zero and two poles. As in Section III, a very high-frequency zero created by $C_{g s}$ of $M_{1}$ is ignored

$$
\begin{equation*}
G_{\mathrm{CLP}}(s)=\frac{\left(a_{\mathrm{PRP}} / C_{X} C_{L}\right)\left(1+\sqrt{2} s C_{x} g_{m} / a_{\mathrm{PRP}}\right)}{\left(s^{2}+2 \xi \omega_{n \mathrm{PRP}} s+\omega_{n \mathrm{PRP}}^{2}\right)} \tag{5}
\end{equation*}
$$

where

$$
\begin{aligned}
a_{\mathrm{PRP}} & =\left(G_{L} \sqrt{2} g_{m}+g_{m}^{2} / \sqrt{2}\right) \\
2 \xi \mathrm{FRP} \omega_{n \mathrm{PRP}} & =\left(1.2 \sqrt{2} g_{m} / C_{L}+G_{L} / C_{X}\right) \\
\omega_{n \mathrm{PRP}}^{2} & =\left(1.2 \sqrt{2} g_{m} G_{L}+g_{m}^{2} / \sqrt{2}\right) /\left(C_{X} C_{L}\right)
\end{aligned}
$$

Here, it is assumed that $G_{L}=1 / R_{L}, C_{\mathrm{gs}}$ and $C_{x} \ll C_{L}$, $g_{m} \gg g_{\mathrm{o}}$, and $G_{L}>g_{\mathrm{o}}$. The zero of the circuit associated with


Fig. 7. Small signal model of PRP-AB-VF.


Fig. 8. Root locus of PRP-AB-VF as a function of open-loop gain $A_{\mathrm{OL}}=g_{m} R_{L}$.
node $V_{X}$ is given by $\omega_{\mathrm{ZPRP}}=\left(G_{L} / C_{X}\right)+\left(g_{m} / 2 C_{X}\right)$. As in the previous circuit, $C_{X}$ is very small, and for this reason, $\omega_{\text {ZPRP }}$ also remains at high frequency and does not have a significant effect on the transfer function. The damping ratio $\xi_{\text {PRP }}$ and $\omega_{\text {nPRP }}$ can be expressed, respectively, as shown in

$$
\begin{align*}
\xi_{\mathrm{PRP}} & =\left(1.2 \sqrt{2} g_{m} / C_{L}+G_{L} / C_{X}\right) /\left(2 \omega_{n \mathrm{PRP}}\right)  \tag{6}\\
\omega_{n \mathrm{PRP}} & =\sqrt{\left(1.2 \sqrt{2} g_{m} G_{L}+g_{m}^{2} / \sqrt{2}\right) / C_{X} C_{L}} . \tag{7}
\end{align*}
$$

The root locus of the proposed VF is given in Fig. 8 for similar conditions as in Section III: bias current $I_{B}=50-\mu \mathrm{A}, \pm 0.6-\mathrm{V}$ supply voltage, and equal $W / L(15 / 0.15)$ (in $\mu \mathrm{m}$ ) of all transistors.

Similar as in the CNV-AB-VF with increasing loop gain $g_{m} R_{L}$, the poles move toward each other, and after $g_{m} R_{L}$ reaches a certain value, they become complex conjugate. In the design example, poles become complex conjugate for openloop gains $g_{m} R_{L}>8$, as shown in Fig. 8. When poles are complex conjugates, the BW of the PRP-AB-VF can be obtained from (2). For the proposed circuit when there is no overshoot in the transient response, the value of $\xi_{\text {PRP }}=0.73$,


Fig. 9. BW of PRP-AB-VF and CNV-VF as a function of $g_{m} R_{L}$.


Fig. 10. Maximum positive output current PRP-AB-VF and CNV-VF for varying $g_{m} R_{L}$
$g_{m} R_{L}=11$, and $Q=0.68$. In this condition, the maximum BW without peaking in the frequency response is $\mathrm{BW}_{\mathrm{PRP}-\mathrm{AB}-\mathrm{VF}}=0.96 \omega_{\mathrm{nPRP}} / 2 \pi$. The numerical value of the BW can be determined by inserting values of $\xi_{\text {PRP }}$ and $\omega_{\text {nPRP }}$ into (2). The value of $\omega_{\mathrm{nPRP}}$ can be calculated by inserting the values $g_{m}=836 \mu \mathrm{~A} / \mathrm{V}^{2}, C_{X}=0.1 \mathrm{pF}, C_{L}=20 \mathrm{pF}$, and $R_{L}=13 \mathrm{k} \Omega$ in (7). Thus, the BW of PRP-AB-VF for $\xi_{\text {PRP }}=0.73$ is 84 MHz , which is 12 times higher than the BW of the CNV-VF and allows a large positive output current independent of $g_{m} R_{L}$ as shown in Figs. 9 and 10. Fig. 11 shows the simulation of the input impedance of the PRP-AB-VF and CNV- VF. It can be observed that the input impedance has a slope of -20 dB and $-90^{\circ}$ phase from 1 kHz to 25 MHz . This implies that the input impedance is mainly capacitive for frequencies from 1 kHz to 25 MHz . The input impedance corresponds to an extremely large resistance $R_{\text {in }} \sim 400 \mathrm{G} \Omega$ in parallel with an extremely small capacitor $C_{\text {in }} \approx 7 \mathrm{fF}$ over a very wide BW. Hence, it will have a minimal loading effect on the response of the circuit where it will be used as a buffer. The analytical expression of the input impedance is given in the Appendix.

## V. Comparison of Followers

In this section, the response of the proposed VF is compared with the CNV-AB-VF to demonstrate the significant advantage of the former predicted by the small signal analysis and simulation results. The experimental verification results are given in Section VII. The effective speed of the VF depends on both the BW and the SR. The BW determines the exponential


Fig. 11. Input impedance magnitude and phase for $C_{L}=20 \mathrm{pF}$.


Fig. 12. Comparison of BW of VFs as a function of $g_{m} R_{L}$.
component of the settling time, while the SR determines the linear component of the settling time. To reduce the settling time, both the BW and the SR need to be improved simultaneously. It is also desirable to have approximately equal maximum positive and negative output currents in order to have symmetrical SRs. This is important, since as indicated Section I, the minimum of the positive and negative SRs determines the SR of the circuit. From Fig. 12, it is observed that increasing $R_{L}\left(g_{m} R_{L}\right)$ provides large BW enhancement for the CNV-AB-VF with respect to class A CNV-VF in Fig. 1. However, Fig. 13 shows that despite providing a larger negative output current, the CNV-AB-VF has very low positive output current for a large $R_{L}$ value, which degrades the positive SR given by $\mathrm{SR}^{+}=d V_{\mathrm{Out}} / d t=I_{\mathrm{Out}}^{+} / C_{L}$. The output current can be expressed as $I_{\text {Out }}^{+}=\mathrm{SR} \cdot C_{L}$. The PRP-$\mathrm{AB}-\mathrm{VF}$ provides a consistently high maximum positive (and negative) output current for all the values of $R_{L}\left(g_{m} R_{L}\right)$ with the same bias current. This is because of the transistor $M_{1 \mathrm{AB}}$ in Fig. 2(c), which acts as a CNV-VF and can provide a large maximum positive output current independent on the value of $R_{L}$. For $g_{m} R_{L}=11\left(\xi_{\mathrm{PRP}}=0.73\right)$, the positive and negative currents are equal in the PRP-AB-VF. Thus, almost symmetric SR can be obtained from the proposed VF. Fig. 14(a) and (b)


Fig. 13. Maximum positive and negative current of PRP-AB-VF and CNV-AB-VF for varying $g_{m} R_{L}$.


Fig. 14. Transient response of CNV-AB-VF and PRP-AB-VF for (a) $R_{L}=13 \mathrm{k} \Omega$ and (b) $R_{L}=1 \mathrm{k} \Omega$.
shows the transient responses of the CNV-AB-VF and the PRP-AB-VF for $R_{L}=13 \mathrm{k} \Omega$ and $R_{L}=1 \mathrm{k} \Omega$, respectively. These are for a $500-\mathrm{mV}$ peak-to-peak $1-\mathrm{MHz}$ input square pulse, and $C_{L}=20 \mathrm{pF}$. Fig. 14 depicts that for large $R_{L}$ values, the positive SR of $\mathrm{CNV}-\mathrm{AB}-\mathrm{VF}$ deteriorates while both the positive and negative SRs of the PRP-AB-VF remain high, whereas for small $R_{L}=1 \mathrm{k} \Omega$ values, as expected, the negative SR of both the circuits deteriorates. This validates that the simultaneous improvement of positive and negative SRs and BW is not possible in the CNV-AB-VF.


Fig. 15. Simulated output impedance of PRP-AB-VF and CNV-VF for nonideal source.


Fig. 16. Frequency response of the PRP-AB-VF for nonideal source where $R_{S}$ is parameterized from 1 to $100 \mathrm{k} \Omega$ for $C_{L}=50 \mathrm{pF}$.

From Figs. 4 and 8, it is observed that for increasing $g_{m} R_{L}$, the complex poles of the previously reported CNV-AB-VF are closer to the imaginary axis than the PRP-AB-VF. Thus, the CNV-AB-VF has a lower damping ratio ( $\xi$ ) than the proposed one. The lower damping ratio leads to a higher overshoot in the transient response of the circuit. The damping ratio ( $\xi$ ) for the CNV-AB-VF is less than 0.7 for an open-loop gain of 9 , whereas the damping ratio for the proposed VF is less than 0.7 for an open-loop gain of 12 . Hence, the openloop gain of the PRP-AB-VF can be increased to a value $g_{m} R_{L}=11$, without overshoot in the transient response. Consequently, it will help to increase even further the BW of the circuit keeping symmetrical and improved SR.

## VI. Proposed AB-VF With Nonideal Source

The application considered in this paper for the proposed VF is to serve as a buffer for amplifiers. The internal resistance of the signal source $R_{S}$ and the $C_{\text {gs1P }}$ neglected in the derivation of Section IV might affect the response of the follower as reported in [13]-[15]. In this section, we showed that $R_{S}$ and $C_{\mathrm{gs} 1 \mathrm{P}}$ have negligible effect in the transient and magnitude response of the PRP-AB-VF over a wide range


Fig. 17. Frequency response of the PRP-AB-VF for nonideal source with $R_{S}$ parameterized from 1 to $100 \mathrm{k} \Omega$ for $C_{L}=10 \mathrm{pF}$.


Fig. 18. Transient response of the PRP-AB-VF for nonideal source with $R_{S}$ parameterized from 1 to $100 \mathrm{k} \Omega$ for $C_{L}=50 \mathrm{pF}$.
of $R_{S}$ values for the range of $C_{L}$ values considered here. The simulated output impedance of PRP-AB-VF and CNVVF, magnitude, and transient responses of the PRP-AB-VF are shown in Figs. 15-19. The simulations have been performed considering a nonideal source to evaluate the effect of a nonideal source with nonzero internal resistance $R_{S}$. The values of $R_{S}$ were parameterized from 1 to $100 \mathrm{k} \Omega$. From Fig. 15, it can be observed that the CNV-VF has a constant $630-\Omega$ output impedance, whereas the PRP-AB-VF has $100-\Omega$ output impedance over the frequency range of 226 kHz to 50 MHz for the ideal source. The output impedance starts to decrease after 226 kHz because of the cutoff frequency $f_{0}=$ $1 / R_{\text {large }} C_{\mathrm{BAT}}$ of the combination of $R_{\text {large }}$ and $C_{\mathrm{BAT}}$, which provides the dynamic class AB operation. From Fig. 15, it can be asserted that as the frequency increases, the value of $Z_{\text {Out }}$ approaches $R_{S}$ as expected [12]. The analytical expression of the output impedance is given in the Appendix. Regarding the magnitude response from Fig. 16, it can be asserted that the PRP-AB-VF has no peaking in the frequency response up to source resistances with value $R_{S}=100 \mathrm{k} \Omega$ when $C_{L}=50 \mathrm{pF}$.


Fig. 19. Transient response of the PRP-AB-VF for nonideal source where $R_{S}$ parameterized from 1 to $100 \mathrm{k} \Omega$ for $C_{L}=10 \mathrm{pF}$.

TABLE I
THD at Six Different Corners and Their SDs

| Corner | $\begin{aligned} & \text { THD } \\ & \text { PRP-AB- } \\ & \text { VF (\%) } \end{aligned}$ | S.D. | $\begin{aligned} & \text { THD } \\ & \text { CNV- } \\ & \text { AB-VF } \\ & (\%) \\ & \hline \end{aligned}$ | S.D. | $\begin{gathered} \text { THD } \\ \text { CNV- } \\ \text { VF } \\ (\%) \\ \hline \end{gathered}$ | S.D. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| tt | 0.27 | 0.03 | 0.52 | 0.03 | 1.54 | 0.16 |
| fs | 0.22 |  | 0.54 |  | 1.50 |  |
| sf | 0.32 |  | 0.53 |  | 1.64 |  |
| Ss | 0.26 |  | 0.55 |  | 1.72 |  |
| ff | 0.28 |  | 0.51 |  | 1.42 |  |
| ssf | 0.25 |  | 0.58 |  | 1.86 |  |

However, for the lower value of $C_{L}$, it has moderate peaking for $R_{S}=70 \mathrm{k} \Omega$ in Fig. 17. Figs. 18 and 19 show the transient response of the PRP-AB-VF for $C_{L}=50$ and 10 pF at a $1-\mathrm{MHz}$ square pulse generated by a nonideal signal source. It can be seen that for a larger source resistance, the overshoots in the transient response become lower with the increase in $C_{L}$ value. Hence, an amplifier with a relatively large output impedance can be interfaced with the PRP-AB-VF for load capacitances with values $C_{L}>10 \mathrm{pF}$ without introducing significant peaking. The small signal model of PRP-AB-VF with nonideal source and $C_{\mathrm{gs} 1 \mathrm{P}}$ is given in the Appendix.

## VII. Experimental/Simulation Results

The PRP-AB-VF, CNV-AB-VF, and CNV-VF were fabricated in a $0.13-\mu \mathrm{m}$ CMOS n-well process with $15 / 0.15$-unit transistor size $($ in $\mu \mathrm{m}), R_{\text {large }}=500 \mathrm{k} \Omega$, and $C_{\mathrm{BAT}}=2-\mathrm{pF}$ capacitor. The CNV-AB-VF was fabricated with $R_{L}=1 \mathrm{k} \Omega$ $\left(g_{m} R_{L}=0.8\right)$. A value of $R_{L}=13 \mathrm{k} \Omega\left(g_{m} R_{L}=11\right)$ was used for the PRP-AB-VF. This value leads to a maximum BW and symmetrical SR also, as explained in Section V. The circuits were tested and simulated with $R_{S}=50 \Omega$, a bias current $I_{B}=50 \mu \mathrm{~A}$, dual supply voltages $\pm 0.6 \mathrm{~V}$, and $C_{L}=50 \mathrm{pF}$. The load resistance $R_{L}$ of the proposed VF is implemented with a PMOS transistor operated in the triode region with dimensions (in $\mu \mathrm{m}$ ) 0.9/0.18 with the gate connected to a bias voltage $V_{\text {bias }}=-100 \mathrm{mV}$. Fig. 20 shows the simulated transient response of the PRP-AB-VF for 500mv peak-to-peak 1-MHz input sinusoidal signal at six different corners.


Fig. 20. Simulated transient response of PRP-AB-VF at six different corners for $1-\mathrm{MHz} 500-\mathrm{mV}$ peak-to-peak sinusoidal signal.


Fig. 21. Experimental frequency response of PRP-AB-VF, CNV-AB-VF, and CNV-VF for $50-\mathrm{pF}$ load capacitance.

Table I shows the simulated total harmonic distortion (THD) of the PRP-AB-VF, the CNV-AB-VF, and the CNV-VF at six different corners. The standard deviations (SDs) of the THD at six different corners are also shown in Table I for CNV-VF, CNV-AB-VF, and PRP-AB-VF. The THD of the proposed VF is lower than that of the CNV-VF and of the CNV-AB-VF for $500-\mathrm{mv}$ peak-to-peak 1-MHz sinusoidal input signal, as it has a higher SR than previously stated VFs.

Fig. 21 shows the experimental frequency response of the PRP-AB-VF, CNV-AB-VF, and CNV-VF. Fig. 22 shows the experimental transient response of the CNV-VF, CNV-AB-VF, and the PRP-AB-VF for a $1-\mathrm{MHz}$ ( $500-\mathrm{mV}$ peak-to-peak amplitude) input pulse. The PRP-AB-VF has an experimental BW value $\mathrm{BW}_{\mathrm{PRP}-\mathrm{AB}-\mathrm{VF}}=50 \mathrm{MHz}$ with $C_{L}=50 \mathrm{pF}$, while the BW of the CNV-AB-VF is $\mathrm{BW}_{\mathrm{CNV}-\mathrm{AB}-\mathrm{VF}}=18 \mathrm{MHz}$. The BW of CNV-VF is 3.4 MHz . From the experimental transient response, it can be observed that the PRP-AB-VF has the highest negative SR compared with the CNV-AB-VF.

At the value of $R_{L}=1 \mathrm{k} \Omega\left(g_{m} R_{L}=0.8\right)$, the CNV-$\mathrm{AB}-\mathrm{VF}$ has a maximum positive output current and a low negative current [shown in Figs. 13 and 14(b)] and the BW

TABLE II
Performance Comparison of CNV-VF, CNV-AB-VF, and PRP-AB-VF With Other Class AB VFs in Literature

| Parameter | CNV-VF <br> Fig. 1 | Ref [4] | $\begin{aligned} & \text { Ref [10] } \\ & \text { (CNV-AB-VF) } \\ & \text { Fig. } 2 \mathrm{~b} \end{aligned}$ |  | Ref [16] |  | Ref [17] |  | Ref [18] | Ref[6] | Ref [19] Fig.2c | This work <br> (PRP-AB- <br> VF) <br> Fig. 2c |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Exp | $\begin{aligned} & \text { Exp } \\ & \mathrm{AB} \# 1-3 \end{aligned}$ | $\begin{aligned} & \hline \text { Exp } \\ & \text { In Ref [6] } \end{aligned}$ | $\begin{array}{ll} \hline \text { Exp } & \\ \text { In } \\ \text { work } & \\ \hline \end{array}$ | Sim | Simulated by authors | Exp | Simulated by authors | Exp | Exp | Exp | Exp |
| Process technology | $\begin{aligned} & \text { CMOS } \\ & 0.13 \mu \mathrm{~m} \end{aligned}$ | CMOS $0.5 \mu \mathrm{~m}$ | ALD1106 <br> Tran. <br> Array | $\begin{aligned} & \text { CMOS } \\ & 0.13 \mu \mathrm{~m} \end{aligned}$ | CMOS 0.5 $\mu \mathrm{m}$ | $\begin{aligned} & \text { CMOS } \\ & 0.13 \mu \mathrm{~m} \end{aligned}$ | CMOS 0.35 $\mu \mathrm{m}$ | CMOS 0.13 $\mu \mathrm{m}$ | $\begin{aligned} & \text { CMOS } \\ & 0.35 \\ & \mu \mathrm{~m} \end{aligned}$ | CMOS 0.18 $\mu \mathrm{m}$ | $\begin{aligned} & \text { CMOS } \\ & 0.5 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & \text { CMOS } \\ & 0.13 \mu \mathrm{~m} \end{aligned}$ |
| Supply (V) | $\pm 0.6$ | $\pm 1.65$ | 2.7 | $\pm 0.6$ | $\pm 1.5$ | $\pm 0.6$ | 3 | $\pm 0.6$ | 3.3 | $\pm 0.9$ | $\pm 1.65$ | $\pm 0.6$ |
| $\mathrm{I}_{\text {Bias }}(\mu \mathrm{A})$ | 50 | 10 | 55 | 50 | 30 | 50 | 10 | 50 | 500 | 30 | 10 | 50 |
| Load Cap (pF) | 50 | 30 | 280 | 50 | 10 | 50 | 20 | 50 | 12 | 50 | 30 | 50 |
| BW(MHz) | 3.4 | $\begin{aligned} & \hline 8.4- \\ & 13.4 \end{aligned}$ | 2 | 18 | 70 | 46 | 5.8 | 6.16 | 87 | 32 | 13.1 | 50 |
| $\mathrm{I}_{\text {out }}^{\text {Max }+}$ (mA) | 0.95 | $\begin{aligned} & \hline 0.6- \\ & 0.87 \end{aligned}$ | 0.92 | 0.9 | 0.850 | 2.1 | 1.62 | 3.1 | 2.4 | 1.3 | 0.75 | 0.975 |
| $\mathrm{I}_{\text {out }}{ }^{\text {Max- }}$ (mA) | 0.075 | $\begin{aligned} & 0.51- \\ & 1.05 \end{aligned}$ | 0.54 | 0.16 | 0.525 | 1.7 | 1.67 | 3.2 | NA | 1.01 | NA | 1.33 |
| $\mathrm{SR}^{+}(\mathrm{V} / \mu \mathrm{S})$ | 19 | 20-29 | 3.75 | 18 | 85 | 60 | 79.4 | 62 | 200 | 25.6 | 25 | 19.5 |
| SR-(V/ $\mu \mathrm{S}$ ) | 1.5 | 17-35 | 1.82 | 3.2 | 52.5 | 35 | 83.6 | 64 | NA | 20.1 | NA | 26.75 |
| Input noise <br> spectral density <br> $@ 1 \mathrm{MHz}$  <br> $(\mathrm{nV} / \sqrt{ } \mathrm{Hz})$  | $\begin{aligned} & 18 \\ & \text { (simulated) } \end{aligned}$ | 30-55 | NA | $\begin{aligned} & 16 \\ & \text { (simulated) } \end{aligned}$ | NA | NA | NA | NA | NA | NA | 40 | $\begin{aligned} & 16 \\ & \text { (simulated) } \end{aligned}$ |
| Silicon area $\left(\mathrm{mm}^{2}\right)$ | 0.002 | $\begin{aligned} & 0.014- \\ & 0.025 \end{aligned}$ | NA | 0.0067 | NA | NA | 0.014 | NA | 0.0097 | 0.013 | 0.011 | 0.0074 |
| Quiescent power $\mathrm{P}^{\mathrm{Q}}(\mu \mathrm{Watt})$ | 60 | $\begin{aligned} & 165- \\ & 198 \end{aligned}$ | 148.5 | 60 | 198 | 168 | 243 | 486 | 3300 | 229 | 99 | 60 |
| $\mathrm{FOM}_{\mathrm{CE}}=$ <br> $\mathrm{I}_{\text {outMAX }} / \mathrm{I}_{\text {Qtotal }}$ | 1.5 | 10-14.5 | 9.8 | 3.2 | 7.5 | 12 | 20 | 8 | 2.4 | 8 | 25 | 19.5 |
| $\begin{aligned} & \mathrm{FOM}_{\mathrm{BW}}=(\mathrm{BW} * \\ & \mathrm{C}_{\mathrm{L}} / \mathrm{P}^{\mathrm{Q}} \\ & {[(\mathrm{MHz}) \mathrm{pF}] / \mu \mathrm{W}} \end{aligned}$ | 2.8 | $\begin{aligned} & 1.5- \\ & 2.03 \end{aligned}$ | 3.77 | 15 | 3.53 | 13 | 0.47 | 0.62 | 0.32 | 7 | 3.96 | 41.6 |
| $\begin{aligned} & \mathrm{FOM}_{\mathrm{GLB}}= \\ & \sqrt{\mathrm{FOM}_{\mathrm{BW}} \mathrm{FOM}_{\mathrm{CE}}} \end{aligned}$ | 2.04 | $\begin{aligned} & \hline 3.87- \\ & 5.43 \end{aligned}$ | 6.07 | 6.9 | 5.14 | 12.8 | 3.06 | 2.22 | 0.87 | 7.5 | 9.94 | 28 |

is also less than the PRP-AB-VF (shown in Fig. 12). Hence, the experimental transient and frequency response validate the theoretical claim.

The simulated input noise spectral density of CNV-VF, CNV-AB-VF, and PRP-AB-VF is given in Table II. The PRP-AB-VF has $16-\mathrm{nV} / \sqrt{ } / \mathrm{Hz}$ input noise spectral density. Fig. 23 shows settling the response of the PRP-AB-VF at different capacitive loads. A $50-\mathrm{mV}$ amplitude and $1-\mathrm{MHz}$ step signal is applied at the input of the PRP-AB-VF to observe the settling performance of the PRP-AB-VF. For $C_{L}$ of 50 pF , the settling time is 22.4 ns ( $2 \%$ of its final value). From Fig. 23, it can be observed that the transient response has a peak overshoot for a load $C_{L}=5 \mathrm{pF}$. Hence, for that
load, the damping ratio $\xi$ is less than 0.7. It can be asserted that from the settling time response of the PRP-AB-VF, the minimum load capacitance $C_{L}$ of 10 pF it can drive without overshoot in the output response. Fig. 24 shows the simulated transient responses of the CNV-VF, CNV-AB-VF, PRP-AB-VF, and FVF [9] for an input triangular pulse with $900-\mathrm{mV}$ peak-to-peak amplitude and $100-\mathrm{kHz}$ frequency. This exhibits that the AB-FVF of [9] has a serious swing limitation. The PRP-AB-VF has $900-\mathrm{mV}$ output swing, whereas FVF [9] provides only $373-\mathrm{mV}$ output swing.
Table II compares the performance parameters of the conventional, PRP-AB-VF, and several recently published class


Fig. 22. Experimental transient response of PRP-AB-VF, CNV-AB-VF, and CNV-VF for $500-\mathrm{mV}$ amplitude pulse at 1 MHz .


Fig. 23. Settling time for different load capacitances for PRP-AB-VF for $50-\mathrm{mV}$ amplitude square pulse of 1 MHz .

AB buffers [4], [6], [10], [16]-[19]. "Exp" and "Sim" refer to the experimental and simulation results, respectively. The implementation technology and supply voltage can have a significant effect on the performance of a circuit. In this paper, references [16] and [17] were simulated by authors in CMOS $0.13-\mu \mathrm{m}$ technology for a fair comparison. From Table II, it can be observed that the current efficiency figure of merit $\left(\mathrm{FOM}_{\mathrm{CE}}\right)$ of the proposed VF is comparable with [17] in the CMOS $0.35-\mu \mathrm{m}$ technology. However, the small signal figure of merit $\mathrm{FOM}_{\mathrm{BW}}$ of the proposed VF is more than 67 times higher than that of [17] in both the technologies and $\mathrm{FOM}_{\mathrm{CE}}$ is less in the $0.13-\mu \mathrm{m}$ technology. Though $\mathrm{FOM}_{\mathrm{CE}}$ of [19] is also 1.2 times higher than that of the PRP-ABVF, yet $\mathrm{FOM}_{\mathrm{BW}}$ of PRP-AB-VF is 10 times higher than in [19]. The geometric mean of the two figures of merit has been calculated and used as a global speed figure of merit $\left(\mathrm{FOM}_{\mathrm{GLB}}=\left(\mathrm{FOM}_{\mathrm{BW}} \mathrm{FOM}_{\mathrm{CE}}\right)^{1 / 2}\right)$ to compare recently reported buffers and the PRP-AB-VF. The PRP-AB-VF has a


Fig. 24. Input/output range of the VFs.


Fig. 25. Chip micrograph of CNV-AB-VF and PRP-AB-VF.
global speed figure of merit $\mathrm{FOM}_{\text {GLB }}=28$, which is the highest among all circuits. The chip micrograph of the CNV-ABVF and the PRP-AB-VF is shown in Fig. 25. The silicon area consumed by the PRP-AB-VF is $0.0074 \mathrm{~mm}^{2}$, and the CNV-AB-VF is $0.0067 \mathrm{~mm}^{2}$. The CNV-VF occupied $0.002 \mathrm{~mm}^{2}$ of the Si area. The proposed circuit has four times higher FOM $_{\text {GLB }}$, six times higher $\mathrm{FOM}_{\mathrm{CE}}$, and three times higher $\mathrm{FOM}_{\mathrm{BW}}$ compared with the CNV-AB-VF at the expense of only $10 \%$ more Si area than the CNV-AB-VF. Compared with the CNV-VF, the PRP-AB-VF provides 13 times higher $\mathrm{FOM}_{\mathrm{CE}}, 14.8$ times higher $\mathrm{FOM}_{\mathrm{BW}}$, and 13.8 times higher $\mathrm{FOM}_{\text {GLB }}$.

## VIII. Conclusion

A simple modification to a CNV-AB-VF has been shown to significantly improve the positive and negative SRs and the BW, with the same power dissipation and a small additional silicon area with respect to the CNV-VF and the CNV-AB-VF. This has been demonstrated by performing an analytical and experimental comparison of the proposed circuit to the abovementioned VFs. It has been shown that the proposed circuit has the highest global figure of merit of all the VFs reported in the literature. It has 13 times higher current efficiency and 14.8 times higher $\mathrm{FOM}_{\mathrm{BW}}$ than the CNV-VF with the same power dissipation.


Fig. 26. Small signal model of the proposed VF considering $C_{\mathrm{gs} 1 P}$ and nonideal source.

## APPENDIX <br> Expression for Input Impedance, Output Impedance, and $Q$ of Proposed AB-VF

The PRP-AB-VF can be used as an oscillator for low $C_{L}$ values. In this case, $C_{L}$ might not satisfy the condition $C_{L} \gg C g s$ and the small signal model in Fig. 26 will be used considering $g_{m} \gg g_{o}$. From this model, the input impedance $Z_{\text {in }}$ of the follower is given by $(1 \mathrm{~A}) . Z_{\text {in }}$ has a real component that corresponds to a negative frequency-dependent resistance which is important for oscillator applications

$$
\begin{align*}
Z_{\mathrm{in}}(\omega) \approx & -\frac{g_{m 1 \mathrm{P}}^{\prime \prime}}{\left(\omega^{2} C_{L} C_{\mathrm{gs} 1 \mathrm{P}}\right)} \\
& -\frac{g_{m 1 \mathrm{P}} g_{m 2 P}\left(\omega^{2} G_{L} C_{\mathrm{gs} 1 \mathrm{P}} C_{L}\right)}{\left(-\omega^{2} C_{\mathrm{gs} 1 \mathrm{P}} C_{L} G_{L}\right)^{2}+\left(\omega^{3} C_{X} C_{\mathrm{gs} 1 \mathrm{P}} C_{L}\right)^{2}} \\
& +\frac{\left(C_{L}+C_{\mathrm{gs} 1 \mathrm{P}}\right)}{j\left(\omega C_{L} C_{\mathrm{gs} 1 \mathrm{P}}\right)} . \tag{1A}
\end{align*}
$$

$V_{\text {Out }} / V_{\mathrm{S}}$ is a second-order transfer function (not shown here) with $Q$ given by (2A), as shown at the bottom of this page.

Neglecting body effect and assuming $g_{0} \ll g_{m}, Z_{\text {Out }}$ is given by (3A), as shown at the bottom of this page.

Here, $g_{m 1 \mathrm{p}}^{\prime \prime}=g_{m 1}+g_{m 1 \mathrm{P}}$ and $1.2 g_{m 1 \mathrm{P}}^{\prime \prime}=(1+\eta) g_{m 1 \mathrm{P}}^{\prime \prime}$ where $\eta=0.2$ is the body effect coefficient. From the equation of $Z_{\text {Out }}$, it can be observed that at higher frequencies, the output impedance $Z_{\text {Out }}$ is $Z_{\text {Out }} \sim R_{\mathrm{S}}$ which is consistent with simulations shown in Fig. 15.

## REFERENCES

[1] R. G. Carvajal et al., "The flipped voltage follower: A useful cell for low-voltage low-power circuit design," IEEE Trans. Circuits Syst. I, Reg. Papers, vol. 52, no. 7, pp. 1276-1291, Jul. 2005.
[2] A. J. Lopez-Martin, J. Ramirez-Angulo, R. G. Carvajal, and L. Acosta, "Power-efficient class AB CMOS buffer," Electron. Lett., vol. 45, pp. 89-90, Jan. 2009.
[3] J. Ramirez-Angulo, A. J. Lopez-Martin, R. G. Carvajal, and F. M. Chavero, "Very low-voltage analog signal processing based on quasi-floating gate transistors," IEEE J. Solid-State Circuits, vol. 39, no. 3, pp. 434-442, Mar. 2004.
[4] A. L. Martin, J. M. A. Miguel, L. Acosta, J. Ramirez-Angulo, and R. G. Carvajal, "Design of two-stage class AB CMOS buffers: A systematic approach," Etri J., vol. 33, pp. 393-400, Jun. 2011.
[5] M. P. Garde, A. J. Lopez-Martin, and J. Ramirez-Angulo, "Powerefficient class-AB telescopic cascode opamp," Electron. Lett., vol. 54, no. 10, pp. 620-622, 2018.
[6] A. Paul, J. Ramírez-Angulo, and A. Torralba, "Bandwidth-enhanced high current efficiency class-AB buffer with very low output resistance," IEEE Trans. Circuits Syst. II, Exp. Briefs, vol. 65, no. 11, pp. 1544-1548, Nov. 2018.
[7] S. Pourashraf, J. Ramirez-Angulo, A. J. Lopez-Martin, and R. González-Carvajal, "A highly efficient composite class-AB-AB miller op-amp with high gain and stable from 15 pF up to very large capacitive loads," IEEE Trans. Very Large Scale Integr. (VLSI) Syst., vol. 26, no. 10, pp. 2061-2072, Oct. 2018.
[8] E. Cabrera-Bernal, S. Pennisi, A. D. Grasso, A. Torralba, and R. G. Carvajal, "0.7-V three-stage class-AB CMOS operational transconductance amplifier," IEEE Trans. Circuits Syst. I, Reg. Papers, vol. 63, no. 11, pp. 1807-1815, Nov. 2016.
[9] M. Jimenez, A. Torralba, R. G. Carvajal, and J. Ramirez-Angulo, "A new low-voltage CMOS unity-gain buffer," in Proc. IEEE Int. Symp. Circuits Syst., May 2006, p. 4.
[10] J. Ramirez-Angulo, A. J. Lopez-Martin, R. G. Carvajal, A. Torralba, and M. Jimenez, "Simple class-AB voltage follower with slew rate and bandwidth enhancement and no extra static power or supply requirements," Electron. Lett., vol. 42, pp. 784-785, Jul. 2006.
[11] K. Ogata, Modern Control Engineering, 5th ed. Upper Saddle River, NJ, USA: Prentice-Hall, 2010.
[12] B. Razavi, Design of Analog CMOS Integrated Circuits (Electrical and Computer Engineering). New York, NY, USA: McGraw-Hill, 2005.
[13] I. M. Filanovsky, J. Järvenhaara, and N. T. Tchamov, "Source follower: A misunderstood humble circuit," in Proc. IEEE 56th Int. Midwest Symp. Circuits Syst. (MWSCAS), Aug. 2013, pp. 185-188.

$$
\begin{gather*}
Q=\frac{\sqrt{\left(1.2 g_{m 1 \mathrm{P}}^{\prime \prime} G_{L}+g_{m 2 P} g_{m 1 \mathrm{P}}\right)\left[C_{x}\left(C_{L}+C_{\mathrm{gs} 1 \mathrm{P}}\right)+C_{\mathrm{gs} 1 \mathrm{P}} C_{L}\left(G_{L} / G_{S}\right)\right]}}{1.2 g_{m 1 \mathrm{P}}^{\prime \prime} C_{x}+G_{L}\left(C_{L}+C_{\mathrm{gs} 1 \mathrm{P}}\right)}  \tag{2~A}\\
Z_{\mathrm{Out}}=V_{Y} / I_{Y}=\frac{s^{2}\left(C_{x} C_{\mathrm{gs} 1 \mathrm{P}} R_{S}\right)+s\left(C_{\mathrm{gs} 1 \mathrm{P}} R_{S} G_{L}+C_{X}\right)+G_{L}}{s^{2}\left(C_{\mathrm{gs} 1 \mathrm{P}} C_{X}\right)+s\left(C_{\mathrm{gs} 1 \mathrm{P}} G_{L}+C_{X} g_{m 1 \mathrm{P}}^{\prime \prime}\right)+\left(g_{m 2 P} g_{m 1 \mathrm{P}}\right)+g_{m 1 \mathrm{P}}^{\prime \prime} G_{L}} \tag{3~A}
\end{gather*}
$$

[14] J. T. Santos and R. G. Meyer, "A one-pin crystal oscillator for VLSI circuits," IEEE J. Solid-State Circuits, vol. 19, no. 2, pp. 228-236, Apr. 1984.
[15] T. C. Carusone, D. Johns, and K. Martin, Analog Integrated Circuit Design, 2nd ed. Hoboken, NJ, USA: Wiley, 2012.
[16] J. Ramirez-Angulo, S. Gupta, R. G. Carvajal, and A. J. Lopez-Martin, "New improved CMOS class AB buffers based on differential flipped voltage followers," in Proc. IEEE Int. Symp. Circuits Syst., May 2006, pp. 3917-1-3917-4.
[17] C. Sawigun, A. Demosthenous, X. Liu, and W. A. Serdijn, "A compact rail-to-rail class-AB CMOS buffer with slew-rate enhancement," IEEE Trans. Circuits Syst. II, Exp. Briefs, vol. 59, no. 8, pp. 486-490, Aug. 2012.
[18] G. Xing, S. H. Lewis, and T. R. Viswanathan, "Self-biased unity-gain buffers with low gain error," IEEE Trans. Circuits Syst. II, Exp. Briefs, vol. 56, no. 1, pp. 36-40, Jan. 2009.
[19] A. J. Lopez-Martin, E. Osés, J. Ramírez-Angulo, and R. G. Carvajal, "Micropower class AB voltage followers with simple quiescent current control," in Proc. IEEE 55th Int. Midwest Symp. Circuits Syst. (MWSCAS), Aug. 2012, pp. 218-221.


Anindita Paul (M'16) was born in Chinsurah, India. She received the M.Tech. degree in VLSI design from the Institute of Radio Physics and Electronics, University of Calcutta, Kolkata, India. She is currently working toward the Ph.D. degree at the Klipsch School of Electrical Engineering, New Mexico State University, Las Cruces, NM, USA.
Her current research interests include low-voltage low-power analog circuit design.


Jaime Ramírez-Angulo (M'82-F'00) received the B.Sc. degree in communications and electronic engineering (Professional degree) and the M.S.E.E. degree from the National Polytechnic Institute, Mexico City, Mexico, in 1974 and 1976, respectively, and the Ph.D. degree from the University of Stuttgart, Stuttgart, Germany, in 1982.
He was a Professor with Texas A\&M University, College Station, TX, USA. He is currently a Distinguished Award Professor with the Klipsch School of Electrical and Computer Engineering, New Mexico State University, Las Cruces, NM, USA, where he is also the Director of the Mixed-Signal VLSI Laboratory. He is also with the National Institute of Astrophysics, Optics and Electronics (INAOE), Cholula, Mexico. His current research interests include various aspects of design and test of analog and mixed-signal very large-scale integrated circuits.


Antonio Torralba (M'89-SM'02) received the M.Sc. degree in industrial engineering with a minor in electrical engineering and the Ph.D. degree from the University of Seville, Seville, Spain, in 1983 and 1985, respectively.
Since 1983, he has been with the Department of Electronics Engineering, School of Engineering, University of Seville, where he was an Assistant Professor, an Associate Professor from 1987 to 1996, and the Director of the Department from 2008 to 2016. He has also been a Professor with the University of Seville since 1996, where he currently leads a research group on mixed signal design. He was a Visiting Researcher with the Klipsch School of Electrical Engineering, New Mexico State University, Las Cruces, NM, USA, in 1999, and with the Department of Electrical Engineering, Texas A\&M University, College Station, TX, USA, in 2004. He has coauthored 90 papers in international journals. His research interests include low-power low-voltage analog and mixed signal microelectronics.


[^0]:    Manuscript received October 15, 2018; revised January 25, 2019; accepted February 26, 2019. This work was supported by the Spanish Ministry of Economy and Competitiveness under Project TEC2015-71072-C3-3-R. (Corresponding author: Anindita Paul.)
    A. Paul is with the Klipsch School of Electrical and Computer Engineering, New Mexico State University, Las Cruces, NM 88003 USA (e-mail: apaul03@nmsu.edu).
    J. Ramírez-Angulo is with the Klipsch School of Electrical and Computer Engineering, New Mexico State University, Las Cruces, NM 88003 USA, and also with the National Institute of Astrophysics, Optics and Electronics (INAOE), Puebla 72000, Mexico (e-mail: jairamir@nmsu.edu).
    A. Torralba is with the Departamento de Ingeniería Electrónica, Escuela Superior de Ingeniería, University of Seville, 41092 Seville, Spain (e-mail: torralba@us.es).
    Color versions of one or more of the figures in this paper are available online at http://ieeexplore.ieee.org.
    Digital Object Identifier 10.1109/TVLSI.2019.2903116

